

# Epistemic modals, deduction, and factivity

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# *will*

- English *will* has both a purely temporal interpretation and an epistemic interpretation:

(1) Anna **will** be home.

a. Anna will be home at some point in the future, e.g., at 7 pm.

*FUT*✓

b. Given what I know, Anna is home right now.

*EPI*✓

- (a) is a non-modal assertion: there is no uncertainty.
- (b) is a modal assertion: the speaker's best guess based on what she knows so far.

[Condoravdi, 2003]

## cross-linguistically common

- Italian, Romanian, Dutch, Greek, German, French, Spanish ...

(2) Anna **sarà** a casa.  
Anna will-be at home  
'Anna will be at home.'

Italian; *FUT*✓, *EPI*✓

(3) Anna **va** fi acasă.  
Anna will be home  
'Anna will be home.'

Romanian; *FUT*✓, *EPI*✓

[Mihoc, 2014, Giannakidou and Mari, 2018, Ippolito and Farkas, 2018]

## a specialized epistemic future form

- Romanian has a morphological form that is connected to the future BUT only has an epistemic reading:

(4) Anna o fi acasă.  
Anna will be home  
'Anna will be home.'

*FUT*✗, *EPI*✓

- In this talk we will focus on this epistemic use of the future only.

[Mihoc, 2014]

## what is the epistemic future?

- Likened to an epistemic necessity modal:

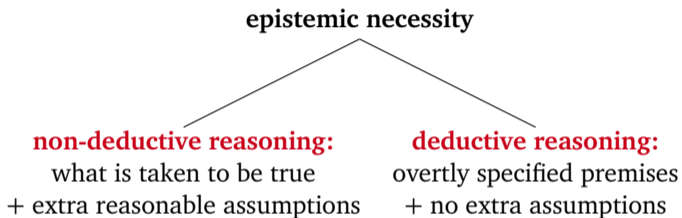
(5)    [[Anna will be home now]] = [[Anna must be home now]]

English: [Condoravdi, 2003]

Romanian: [Mihoc, 2014]

Greek & Italian: [Giannakidou and Mari, 2018]

# epistemic necessity



[Karttunen, 1972, von Fintel and Gillies, 2010, Goodhue, 2017]

## non-deductive vs. deductive

- (6) Context: Anna is conscientious about saving energy. We are passing by her house, and see her lights on. I say: (non-deductive)  
Anna **must** be home now.

(What is taken to be true: light on)

(Extra reasonable assumptions: If light is on, one is at home, Anna wouldn't leave the light on if she's not home)

- (7) If  $x$  is divisible by 2, then  $x$  is even.  
2 is divisible by 2. (deductive)  
So, 2 **must** be even.

(What is taken to be true: If  $x$  is divisible by 2, then  $x$  is even, 2 is divisible by 2)

(No extra assumptions)

[Lassiter, 2016, Goodhue, 2017]

## today: two puzzles

- In a DEDUCTION context, only *must* is felicitous while the epistemic future is not:

(8) If  $x$  is divisible by 2, then  $x$  is even.

2 is divisible by 2.

a. So, 2 **must** be even.

b. #So, 2 **will** be even.

c. #Deci, 2 **va** fi par.  
so 2 VA be even

d. #Deci, 2 **o** fi par.  
so 2 O be even



## today: two puzzles

- In a **FACTIVE** context, again only *must* is felicitous while the epistemic future is not:

- (9)
- I just found out that Anna **must** be in Honolulu now.
  - #I just found out that Anna **will** be in Honolulu now.
  - #Tocmai am aflat că Anna **va** fi în Honolulu acum.  
just have.1SG found.out that Anna VA be in Honolulu now
  - #Tocmai am aflat că John **o** fi în Honolulu acum.  
just have.1SG found.out that Anna O be in Honolulu now

	<i>must</i>	<i>will-EPI/va-EPI / o</i>
deductive context	✓	✗
embedding under factive	✓	✗

## preview

### MAIN QUESTION:

If  $\llbracket \text{epistemic future} \rrbracket = \llbracket \text{epistemic must} \rrbracket$ , then why should these puzzles emerge?<sup>1</sup>

### MAIN IDEAS

- maintain that there is a common core: epistemic necessity semantics [Kratzer 1977, 2012]
- DEDUCTION contexts
  - $p$  is entailed
  - epistemic *must* tolerates an empty ordering source; compatible with entailing  $p$
  - the epistemic future does not and thus does not entail  $p$
- FACTIVE contexts
  - the factive presupposition is interpreted relative to the modal base of the epistemic modal; amounts to a requirement that the modal base should entail  $p$
  - *must* can satisfy the factive presupposition
  - the epistemic future cannot satisfy the factive presupposition

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<sup>1</sup>[Fălăuș and Laca, 2014], [Ippolito and Farkas, 2018] have questioned this claimed equivalence as well.

## modal semantics

(10) Anna **must** be home.

- an EPISTEMIC MODAL BASE  $f$ :

(11)  $f(w) = \{p : p \text{ is taken to be true at } w\}$ ;  $\bigcap f(w) = \{w : w \text{ is in every } p \text{ in } f(w)\}$

- an ORDERING SOURCE  $g$ :

(12)  $g(w) = \{p : p \text{ is a reasonable assumption at } w\}$

- $g(w)$  imposes an ordering on  $\bigcap f(w)$ :

(13)  $\forall w, z \in \bigcap f(w) : w \leq_{g(w)} z \text{ iff } \{p : p \in g(w) \text{ and } w \in p\} \supseteq \{p : p \in g(w) \text{ and } z \in p\}$

- *Best* picks out the  $g(w)$ -best worlds in  $\bigcap f(w)$ :

(14)  $Best(\bigcap f(w), g(w)) = \{w \in \bigcap f(w) : \neg \exists w' \in \bigcap f(w) : w' \leq_{g(w)} w\}$

- universal quantification over *Best*:

(15)  $\llbracket \text{must} \rrbracket^{w,g} = \lambda f_{\langle s, \langle \langle s, t \rangle \rangle \rangle} \cdot \lambda g_{\langle s, \langle \langle s, t \rangle \rangle \rangle} \cdot \lambda p_{\langle s, t \rangle} \cdot \forall w' \in Best(\bigcap f(w), g(w))[p(w')]$

## epistemic *must* and epistemic future

- have the **same truth conditions**:

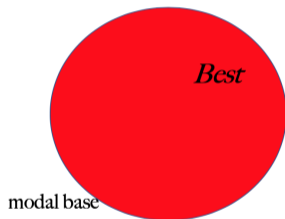
(16)

a.	$\llbracket \text{must} \rrbracket^{w,g}$	$= \lambda f . \lambda g . \lambda p . \forall w' \in \text{Best}(\bigcap f(w), g(w))[p(w')]$
b.	$\llbracket \text{will-EPI/va-EPI/o} \rrbracket^{w,g}$	$= \lambda f . \lambda g . \lambda p . \forall w' \in \text{Best}(\bigcap f(w), g(w))[p(w')]$

- given this shared semantics, why do we see different distributions in deduction and factive contexts?

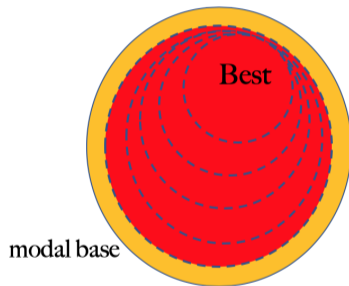
## proposal: deduction

- $f(w)$  = what is taken to be true = just overtly uttered premises
- $g(w) = \emptyset$  (no extra assumptions)
- $Best = \bigcap f(w)$ ,  $w$  is necessarily in  $Best$
- consequence: *[universal modal] p* entails  $p$
- no uncertainty about the validity of  $p$
- this captures the deductive use of *must*



## proposal: non-deduction

- $f(w)$  = what is taken to be true
- $g(w)$  = extra reasonable assumptions
- $Best \subset \bigcap f(w)$ ,  $w$  may not be in  $Best$
- consequence: *[universal modal] p* does not entail  $p$
- uncertainty about the validity of  $p$
- this captures the non-deductive use of *must*

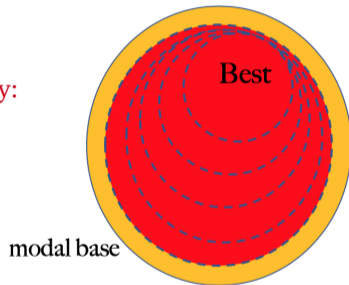


## proposal: epistemic future

- $f(w)$  = what is taken to be true
- $g(w)$  = extra reasonable assumptions
  - crucially, like in the non-deduction case,  $g(w)$  not empty:

(17)  $\llbracket \text{will-EPI/va-EPI/o} \rrbracket^{f,g}$  is defined iff  $g(w) \neq \emptyset$

- $Best \subset \bigcap f(w)$ ,  $w$  may not be in  $Best$
- uncertainty about the validity of  $p$
- captures why the epistemic future is never deductive





## capturing the deduction puzzle

	<i>must</i>	<i>will</i> -EPI/ <i>va</i> -EPI / <i>o</i>
deductive context	✓ $g(w) = \emptyset$	✗ $g(w) \neq \emptyset$
embedding under factive	✓	✗

## prediction about plain assertions

- On our analysis of the deductive use of *must*, *must p* entails *p*.
- Just like a plain assertion!
- Therefore, we predict they can be used interchangeably in such contexts.

- (18) If *x* is divisible by 2, then *x* is even.  
2 is divisible by 2.
- a. 2 **must be** even.
  - b. 2 **is** even.

## factive contexts

- (19) a. I just found out that Anna **must** be in Honolulu now.
- b. #I just found out that Anna **will** be in Honolulu now.
- c. #Tocmai am aflat că Anna **va** fi în Honolulu acum.  
just have.1SG found.out that Anna VA be in Honolulu now
- d. #Tocmai am aflat că John **o** fi în Honolulu acum.  
just have.1SG found.out that Anna O be in Honolulu now

- How is an **epistemic modal** interpreted under a factive predicate?
- How is the **epistemic future** interpreted under a factive predicate?

## factive attitude predicate semantics

- Attitude predicate:

$$(20) \quad \llbracket \text{believe } p \rrbracket^w = \lambda x . \forall w' \in \text{Acc}_{\text{Dox},x}[p(w')]$$

- *Factive* attitude predicate:

$$(21) \quad \llbracket \text{know } p \rrbracket^w = \lambda x : p(w) = 1. \llbracket \text{believe} \rrbracket (p)(x)(w) = 1$$

[Hintikka, 1962, Anand and Hacquard, 2013, Spector and Egré, 2015]

## proposal: factive with modal complement

$$(22) \quad \llbracket \text{know that } \Box p \rrbracket^w = \lambda x : \llbracket \Box p \rrbracket (w) = 1. \llbracket \text{believe that } \Box p \rrbracket (x)(w) = 1$$

- Unpacking the presupposition, we get:

$$(23) \quad \forall w' \in \text{Best}(\bigcap f(w), g(w)) [p(w')] = 1$$

- **Hypothesis:** The factive requires  $g(w) = \emptyset$ .
- The presupposition becomes:

$$(24) \quad \forall w' \in \bigcap f(w) [p(w')] = 1$$

- Putting it all together:

$$(25) \quad \llbracket \text{know that } \Box p \rrbracket^w \\ = \lambda x : \forall w' \in \bigcap f(w) [p(w')]. \llbracket \text{believe that } \Box p \rrbracket (x)(w) = 1$$

## proposal: necessity under factives

$$\begin{aligned} (26) \quad & \llbracket \text{know that must } p \rrbracket^w \\ & = \lambda x : \llbracket \text{must} \rrbracket (p)(w). \llbracket \text{believe that } \Box p \rrbracket (x)(w) = 1 \\ & = \lambda x : \forall w' \in \bigcap f(w)[p(w')]. \llbracket \text{believe that } \Box p \rrbracket (x)(w) = 1 \end{aligned}$$

$$g(w) = \emptyset \checkmark$$

- prediction: it should **able to embed under a factive** only with a **deductive** meaning

$$\begin{aligned} (27) \quad & \llbracket \text{know that will } p \rrbracket^w \\ & = \lambda x : \llbracket \text{will} \rrbracket (p)(w). \llbracket \text{believe that } \Box p \rrbracket (x)(w) = 1 \\ & = \lambda x : \forall w' \in \bigcap f(w)[p(w')]. \llbracket \text{believe that } \Box p \rrbracket (x)(w) = 1 \end{aligned}$$

$$g(w) = \emptyset \times$$

- prediction: it should be **unable to embed under a factive**

## capturing the factivity puzzle

	<i>must</i>	<i>will</i> -EPI/ <i>va</i> -EPI / <i>o</i>
deductive	✓ $g(w) = \emptyset$	✗ $g(w) \neq \emptyset$
embedding under factive <sup>†</sup>	✓ $g(w) = \emptyset$	✗ $g(w) \neq \emptyset$

$$\dagger \forall w' \in \bigcap f(w)[p(w')] = 1$$

## prediction I: possibility under factives

(28) I just found out that Anna **might** be in Honolulu.

- Our hypothesis about the shape of the factive presupposition gives us possibility for free:

(29)  $\llbracket \text{know that } \diamond p \rrbracket^w = \lambda x : \exists w' \in \bigcap f(w)[p(w')] = 1. \llbracket \text{believe that } \diamond p \rrbracket(x)(w) = 1$

- This presupposition merely requires the modal base to be compatible with  $p$ .
- This condition is very easy to meet.
- Captures is why, cross-linguistically, possibility is much easier to embed.<sup>2</sup>

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<sup>2</sup>[Rett, 2012] for English, [Anand and Hacquard, 2014] for Romance.



## prediction II: necessity under non-factive epistemic attitudes

- When the factive presupposition is missing, we do not run into the above problems.
- A variety of non-factive epistemic attitudes can embed these modals.

- (30)
- a. John thinks/believes/suspects Anna **might** be home.
  - b. John thinks/believes/suspects Anna **must** be home.
  - c. John crede/crede/bănuiește că Anna **o** fi acasă  
John thinks/believes/suspects that Anna **o** be home

- Need for more work to identify cross-linguistic patterns of embedding epistemic modals/epistemic future.

## an alternative proposal

- Our solution to the factive puzzle crucially relied on the assumption that the modal in the factive presupposition had to be interpreted only relative to the modal base.
- An alternative would be to say that *know [modal] p* presupposes simply *p*.
- This would give us the *know must p* case:
  - *must p* allows a use where it entails *p*, and therefore satisfies the presupposition.
- This would give us the *know will p* case:
  - *will p* cannot entail *p*, it is unembeddable under a factive.
- But this gives us the wrong result for epistemic possibility:
  - *might p* does not entail *p*, but is very embeddable under factives.

## conclusion

- OVERALL: A comparative analysis of **epistemic future** and **epistemic modality**.
  - revealed crucial differences in deductive and factive contexts, using **Romanian o** as a control
  - maintained a unified core modal semantics
  - derived the differences from restrictions on domains of quantification
- New insights about epistemic *must* along the way.
  - captured both the non-deductive and deductive uses of epistemic *must*
- A compositional account of how an epistemic modal/future interacts with the **factive presupposition**.
  - captured a distributional fact about embedding *must* vs. *might*

## conclusion

- A new **underspecification** account of *must*.<sup>3</sup>
- A unified approach to **deduction and factivity**.
- A **refined** view of the interaction between epistemics and attitudes.

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<sup>3</sup>Ruling out an undesirable lexical ambiguity account.

## outlook

- Why is the future involved in epistemic/temporal ambiguity in language after language?
  - the often non-settled nature of the future makes it a natural choice for uncertainty
  - past morphology often coincides with DIRECT evidentiality cross-linguistically

## outlook

- So far we have looked at contexts where the epistemic future is infelicitous while *must* is not.
- There are cases where the opposite is true! [Fălăuș and Laca, 2014, Ippolito and Farkas, 2018]

(31) a. I don't have the slightest idea, he **#must** be home. (Moore's paradox?)

b. Habar n-am, **o** fi acasă.  
I have no idea, o be home

- The epistemic future is compatible with an assertion of full ignorance, while *must* is not.
- Why?

Thank you!

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